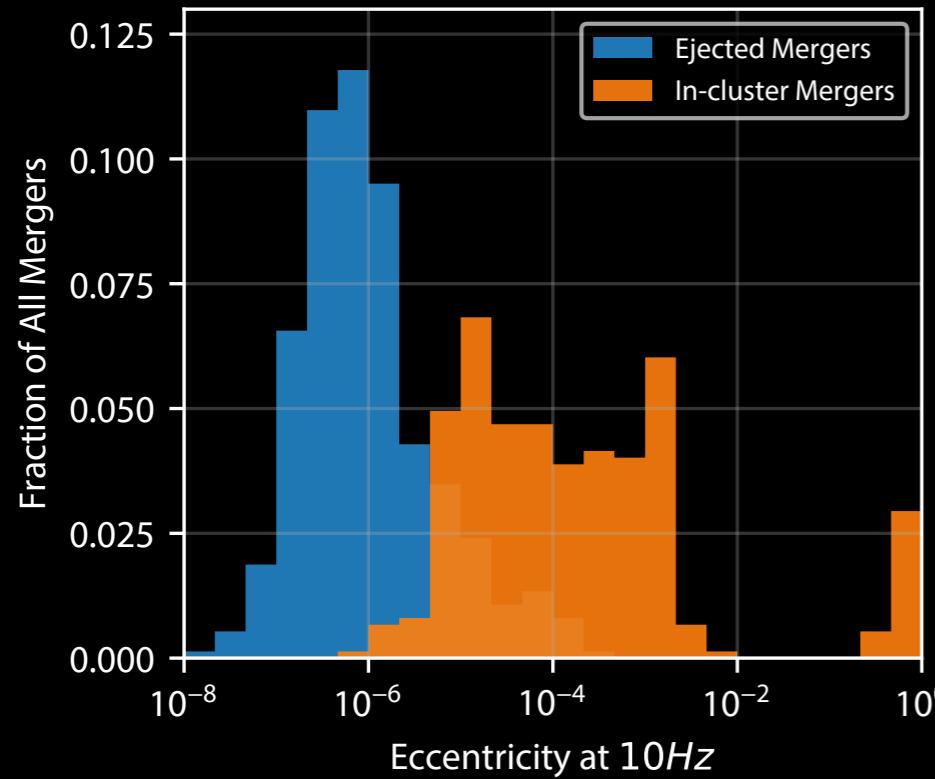


# Multiple Mergers of BHs

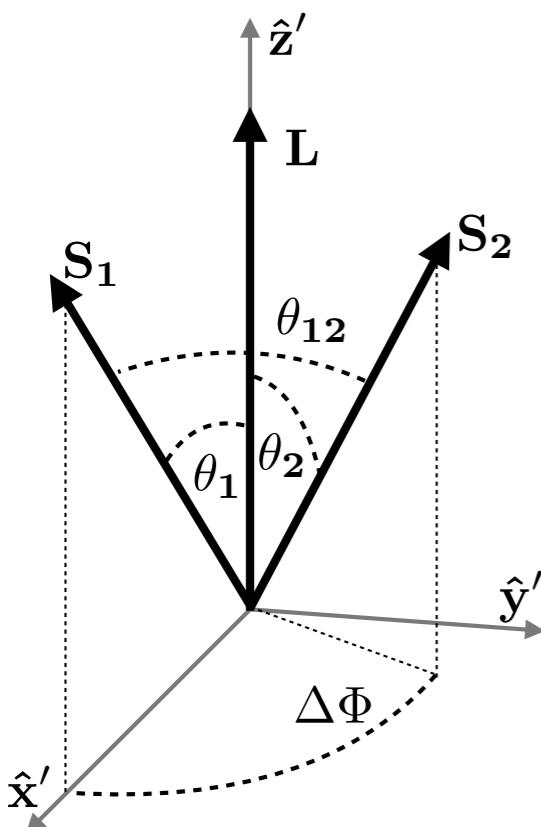


# Beyond effective spins

Davide Gerosa  
NASA Einstein Fellow  
California Institute of Technology



1. **Orbital** motion  $t_{\text{orb}} \propto r^{3/2}$
2. Spin & orbital-plane **precession**  $t_{\text{pre}} \propto r^{5/2}$
3. GW emission and **inspiral**  $t_{\text{GW}} \propto r^4$



...3 evolving variables

$\theta_1, \theta_2, \Delta\Phi$   
(more immediate)

...or equivalently  
(more physical! Timescale separation)

$\chi_{\text{eff}}, \chi_p$   
(useful in waveforms)

# Black Holes Runaway Growth in Globular Clusters

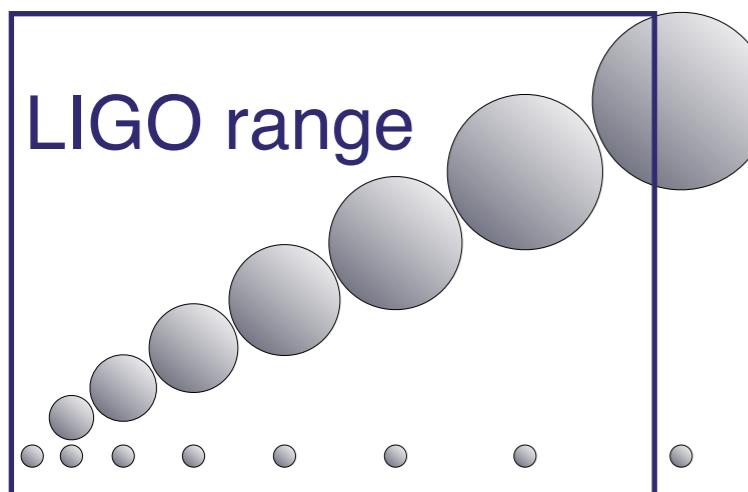
The Question: Are Globular Clusters the birthplaces of merging BHs → GWs?

If yes, then for ~10% of these systems (the most massive and dense) we expect to have a runaway process.

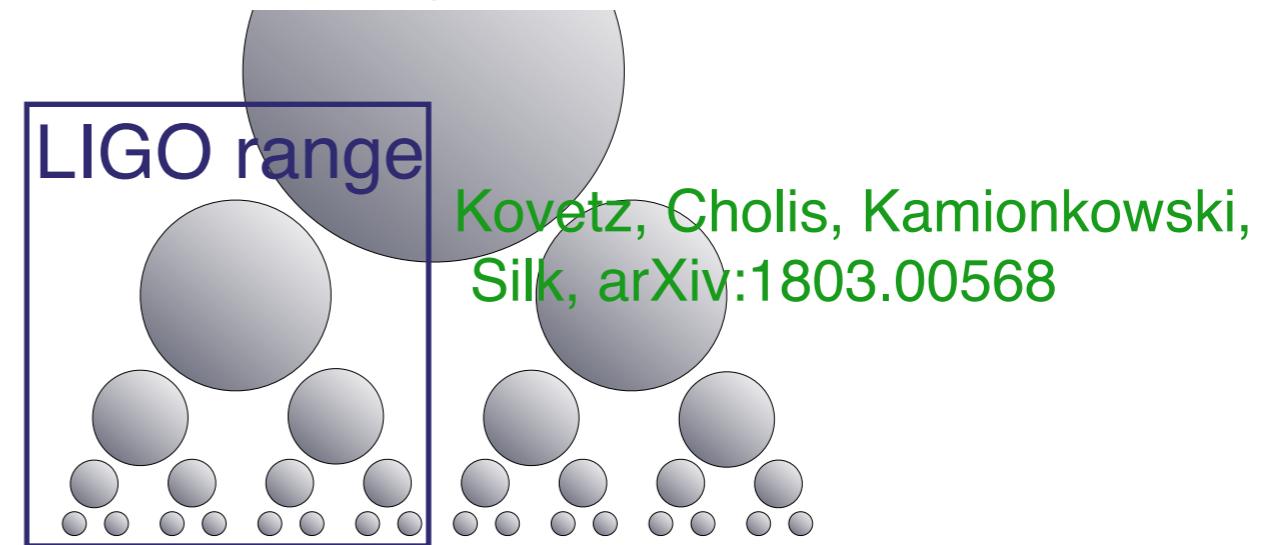
Cholis, Kovetz, Kamionkowski in prep 2018

## Simplified paths:

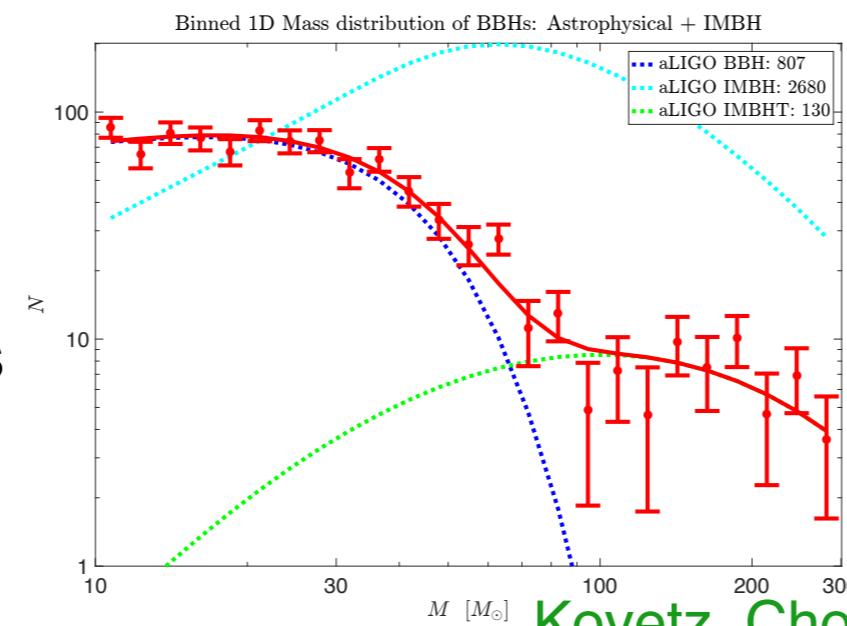
### Top Heavy:



### Bottom Heavy:



From LIGO obs. we will be able to derive limits on the occupation fraction of IMBHs in GCs:



Background Model	Right Triangle			
	O1+O2	O3 (1 yr)	Design (6 yrs)	with $R(z)$
$P(M) \propto \exp(-(M/40)^2)$	470% (0.2)	38% (3)	3.1% (47)	2.9% (53)
$P(M) \propto \exp(-(M/60)^2)$	760% (0.2)	68% (3)	7.4% (47)	6.8% (53)
$P(M) \propto \mathcal{H}(50 - M)$	220% (0.2)	17% (3)	1.3% (47)	1.2% (53)
$P(M) \propto \exp(-M/40)$	890% (0.2)	120% (3)	19% (47)	18% (53)
$\bar{R}_{BG} = 103 + 110 = 213$	470% (0.2)	41% (3)	3.4% (47)	3.1% (53)
$\beta = -1$	430% (0.2)	34% (3)	2.8% (47)	2.7% (53)
$\beta = 1$	480% (0.2)	34% (3)	3.3% (47)	3.1% (53)

Kovetz, Cholis, Kamionkowski, Silk, arXiv:1803.00568

# Next-Gen Numerical Relativity: More Science at Less Cost

Zachariah B. Etienne 

## Reducing human expense

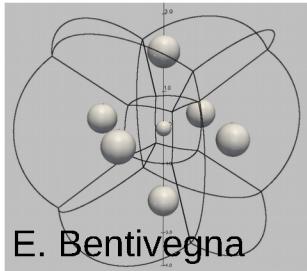
- Lowering learning curve
  - Excellent texts on NR & GW astrophysics
  - Texts on NR codes & algorithms?
    - *Need to improve our code documentation*
- Automatic code generation
  - Input: Eqs in Einstein-like notation
  - Output: Optimized C code
  - Open-source packages
    - Kranc ([kranccode.org](http://kranccode.org))
      - Mathematica-based
    - NRPy+ ([tinyurl.com/nrpyplus](http://tinyurl.com/nrpyplus))
      - Python/SymPy-based

## Reducing computational expense

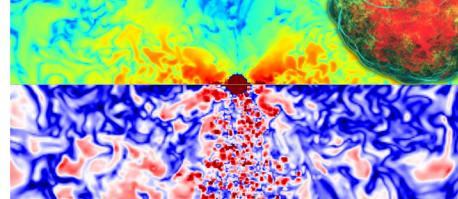
- Moore's Law is slowing
  - Cannot rely on continued CPU speed boosts
- Path forward = more efficient algorithms
  - Better sampling of our spacetimes
    - Beyond Cartesian AMR for CB inspirals:
      - Bispherical-like coords
      - Patches of curvilinear grids
    - Toward implicit timestepping
      - Corotation / dual frame approach
  - More scalable algorithms
    - DG methods
    - Few-patch grids

# Einstein toolkit based results

- binary black hole mergers
- binary neutron star mergers
- mixed binaries
- supernovae
- accretion disks
- boson stars
- cosmology



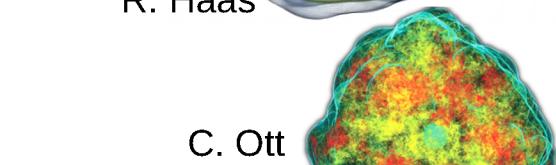
E. Bentivegna



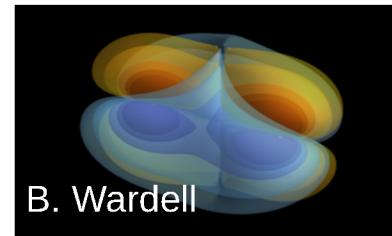
D. Siegel



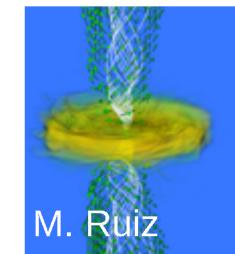
R. Haas



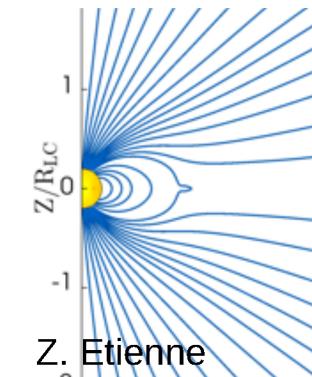
C. Ott



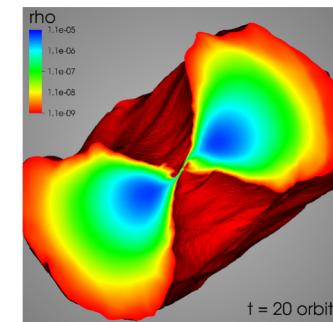
B. Wardell



M. Ruiz



Z. Etienne



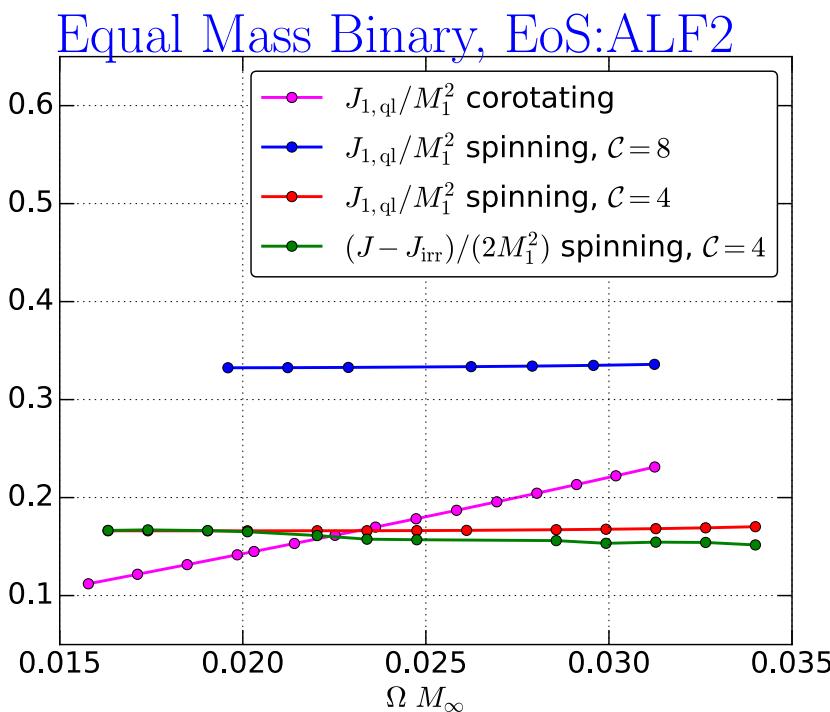
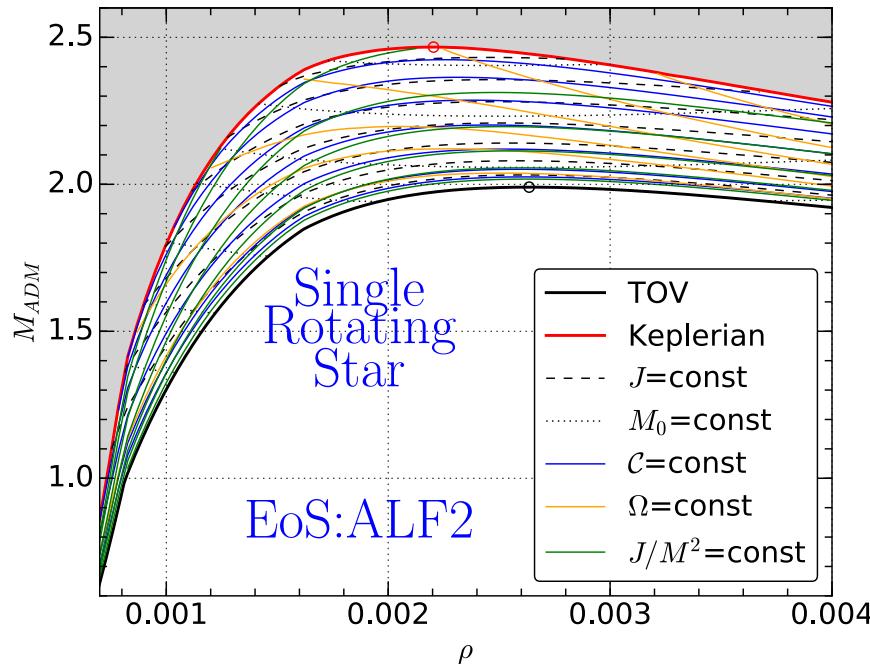
V. Mewes

- GRMHD simulations

- 2 free, open source, mature codes for ideal MHD simulations
- force-free MHD code available
- support for tabulated hot EOS
- neutrino transport: leakage and M1 moment scheme
- fully dynamic gravity solver



# Sequences of spinning binary neutron stars: circulation & spin



Generally lines of constant  $\mathcal{C}$ ,  $J/M^2$  are distinct.

For slow rotations, they nearly coincide (up to a constant)  $\Rightarrow$

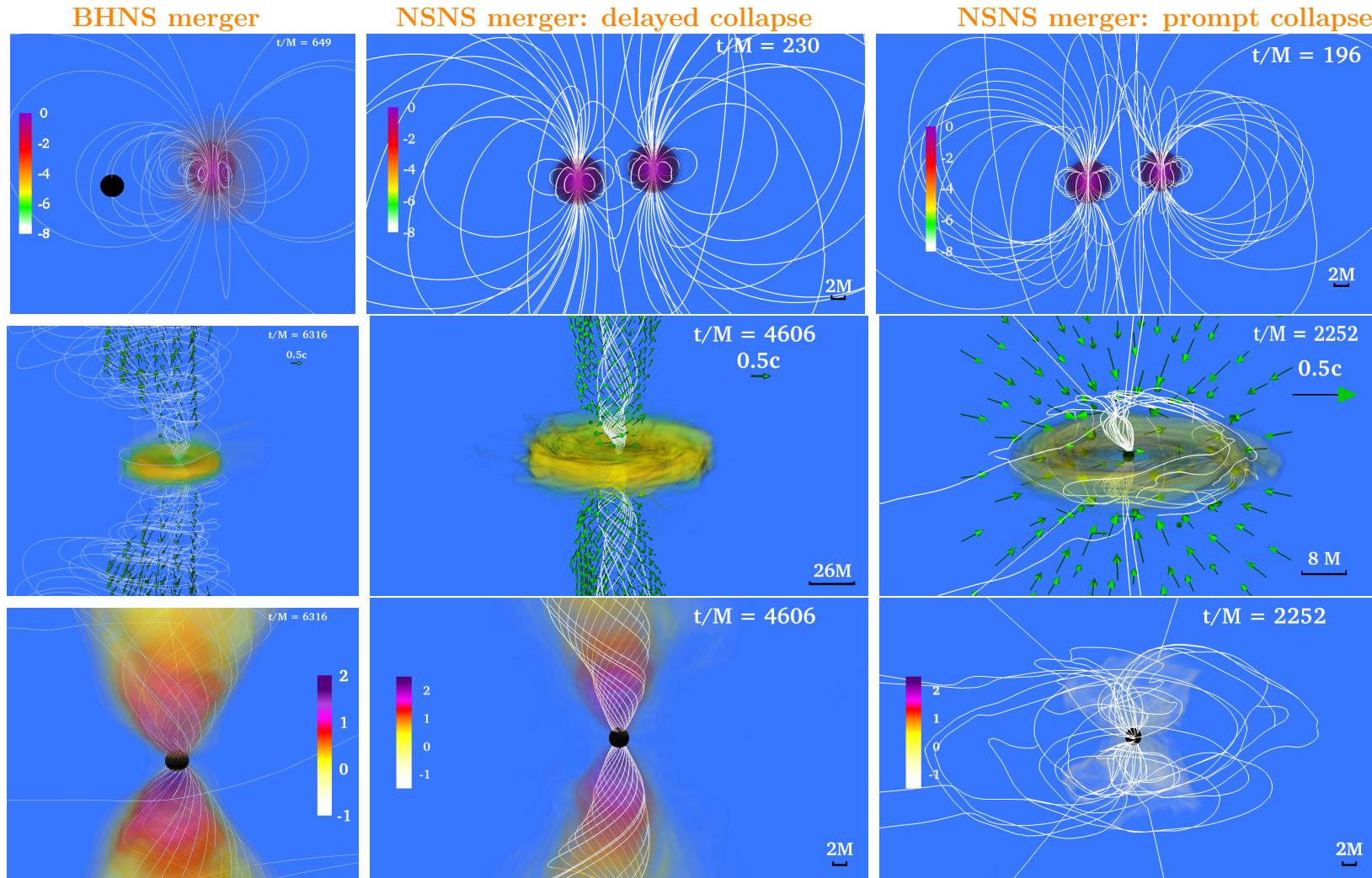
Moving along a  $\mathcal{C} = \text{const}$  curve is almost equivalent to moving along a  $J/M^2 = \text{const}$  curve.

( $J_{1,\text{ql}}$ : Quasi-local angular momentum of one star,  $J$ : Total angular momentum,  $J_{\text{irr}}$ : Total angular momentum of irrotational binary.)

$\Rightarrow$  Corotating sequences can have low spin  $\leq 0.3$  even for close binaries.

$\Rightarrow$  Constant circulation sequences preserve quasi-local spin (for low spins) similarly to single rotating stars.

# GW170817 + GRMHD $\Rightarrow$ NS Maximum Mass<sup>◊</sup>



jet

$$\beta M_{\max}^{\text{sph}} \approx M_{\max}^{\text{sup}} \lesssim 2.74 \lesssim M_{\text{thresh}} \approx \alpha M_{\max}^{\text{sph}}.$$

$$2.74/\alpha \lesssim M_{\max}^{\text{sph}} \lesssim 2.74/\beta$$

EOS causal limit  $\Rightarrow \beta \approx 1.27 \Rightarrow$

$$M_{\max}^{\text{sph}} \lesssim 2.16$$

<sup>◊</sup> M. Ruiz, S. Shapiro, A. Tsokaros, Phys. Rev. D 97, 021501(R) (2018)